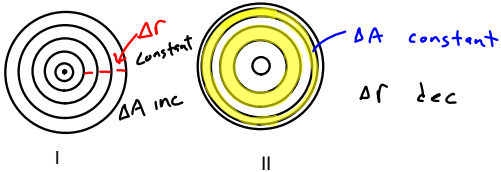


3.4b Other rates of change



Which model best illustrates tree growth if we assume the same amount of new growth each year?

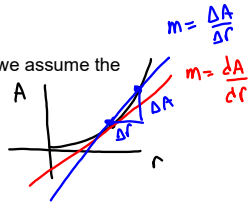
$$A = \pi r^2$$

$$\frac{\Delta A}{\Delta r} \approx \frac{dA}{dr} = 2\pi r$$

$$\frac{\Delta A}{\Delta r} \approx 2\pi r \quad \text{me dec}$$

$$\Delta A \approx 2\pi r \Delta r$$

↑
constant



Sep 20-5:53 PM

Ex 6 p 133 Sensitivity to change in genetics

p = proportion of a dominant gene in a population

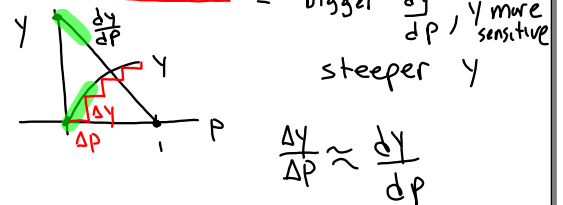
$1-p$ = proportion of the recessive gene

y = proportion of dominant gene in the next generation

$$y = 2p - p^2$$

$$\frac{dy}{dp} = 2 - 2p$$

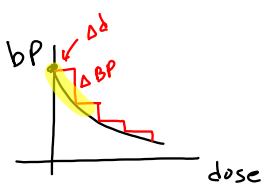
Compare the graphs of y and dy/dp to determine what values of y are more sensitive to a change in p



= bigger $\frac{dy}{dp}$, y more sensitive
steeper y

$$\frac{\Delta y}{\Delta p} \approx \frac{dy}{dp}$$

Sep 20-6:14 PM



Sep 14-9:56 AM

Derivatives in economics

derivative = "marginal"

Ex 7 p 134 Marginal cost and marginal revenue

x = number of radiators per day

$C(x)$ = Total cost to produce all x radiators

$r(x)$ = Total Revenue from x radiators

$P(x)$ = profit = $r(x) - C(x)$

$$C(x) = x^3 - 6x^2 + 15x$$

$$r(x) = x^3 - 3x^2 + 12x$$

marginal cost to produce 10 radiators

$$C'(10) = 300 - 120 + 15 = 195 \approx \text{cost of 11th rad.}$$

$$C'(x) = 3x^2 - 12x + 15$$

$$C(10) = 1000 - 600 + 150 = \$550$$

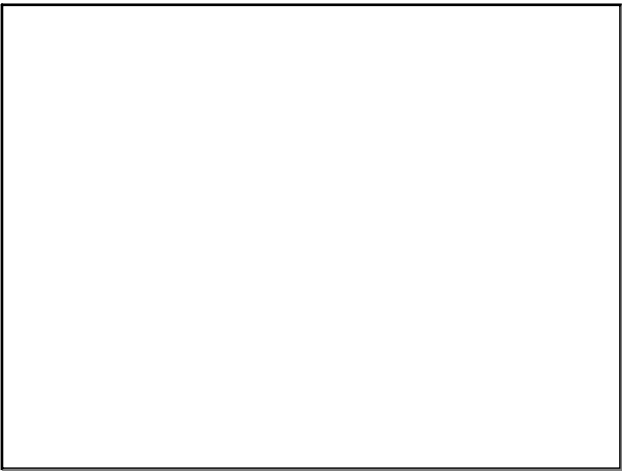
$$r'(10) = 300 - 60 + 12 = 252 \quad C(11) - C(10)$$

$$r'(x) = 3x^2 - 6x + 12$$

$$P'(10) = 252 - 195 = 57$$

revenue for 11th radiator

Sep 20-6:37 PM



Sep 14-10:25 AM